1	i	$\log_{10} P = \log_{10} a + \log_{10} 10^{bt}$ $\log_{10} 10^{bt} = bt$	B1 B1	condone omission of base		
		intercept indicated as log ₁₀ a	B1		3	
	ii	3.9(0), 3.94, 4(.00), 4.05, 4.11 plots ft	T1 P1	to 3 sf or more; condone one error 1 mm		
		line of best fit ft	L1	ruled and reasonable	3	
	iii	(gradient =) 0.04 to 0.06 seen (intercept =) 3.83 to 3.86 seen	M1 M1			
		(a =) 6760 to 7245 seen	A1			
		$P = 7000 \times 10^{0.05t}$ oe	A1	7000×1.12^{t}	4	
	iv	17 000 to 18 500	B2	14 000 to 22 000 B1	2	12

2	(i)	1		
	(ii) –2	2	M1 for $1/9=3^{-2}$ or $\log(1) - \log(3^2)$	
	(iii) $\log x$	2	base not requd; M1 for 5 log x or log(x^6)	5
3	Correct curve thro' y axis (0, 1) indicated on sketch or table	G1 G1	y, y' & y'' all positive independent	
	5.64	3	B2 for other versions of 5.64(3) or B1 for other ans 5.6 to 5.7 or M1 for $x \log 2 = \log 50$ and M1 for $x = \log 50 \div \log 2$	5

4	i	81	1		1
	ii	$(1x)3^{n-1}$	1		1
	iii	(GP with) $a = 1$ and $r = 3$ clear correct use GP sum formula	M1 M1	or M1 for = $1+3+9+ \dots +3^{n-1}$	2
	iv	(A) 6 www (B) B)	2 1	M1 for $364 = (3^n - 1)/2$	3
	v	their (ii) > 900 (y - 1)log 3 > log 900 y - 1 > log 900 \div log 3 y = 8 cao	M1ft M1ft M1 B1	-1 once for = or < seen: condone wrong letter / missing brackets / no base	4

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5	(i)		M1 A1	for curve of correct shape in both quadrants through (0, 1) shown on graph or in commentary	SC1 for curve correct in 1 st quadrant and touching (0,1) or identified in commentary
			[2]		

5	(ii)	$5r - 1 - \frac{\log_{10} 500000}{\log_{10} 10000000000000000000000000000000000$	M1	or $5x - 1 = \log_3 500\ 000$	condone omission of base 10
		$3x - 1 = \frac{1}{\log_{10} 3}$			use of logs in other bases may earn
					full marks
		$x = \left(\frac{\log_{10} 500000}{\log_{10} 3} + 1\right) \div 5$	M1	$x = (\log_3 500000 + 1) \div 5$	
		[x =] 2.588 to 2.59	A1	oe; or B3 www	if unsupported, B3 for correct answer
			[3]		

6	(i	$\log_{10}p = \log_{10}a + \log_{10}10^{kt}$	M1	condone omission of base;	if unsupported, B2 for correct equation
		$\log_{10}p = \log_{10}a + kt \text{ www}$	A1		
			[2]		
6 (ii	2.02, 2.13, 2.23	B1	allow given to more sig figs	2.022304623, 2.129657673, 2.229707433
		plots correct	B1f.t.	to nearest half square	
		ruled line of best fit	B1	y-intercept between 1.65 and 1.7 and at least	ft their plots
				one point on or above the line and at least	must cover range from $x = 9$ to 49
			[3]	one point on or below the line	
6	(;;;	0.0105 to 0.0125 for k	[J]		must be connected to k
U	(III)	0.0105 to 0.0125 tot k	DI		must be connected to k
		1.66 to 1.69 for $\log_{10}a$ or 45.7 to 49.0 for a	B1		must be connected to <i>a</i>
		$\log_{10}p = \text{their } kt + \text{their } \log_{10}a$	B1	must be a correct form for equation of line	
				and with their <i>y</i> -intercept and their gradient	
				(may be found from graph or from table,	
		$1 - \frac{1}{2} = \frac{1}{2} + $	B1	as above "47.9" and "0.0115" must follow	
		$p = \text{their} 47.9 \times 10$ or 10	DI	from correct method	
			[4]		
6	(iv)	45.7 to 49.0 million	1	'million' needed, not just the value of p	
			[1]		
6	(v	reading from graph at 2.301	M1*	or $\log_{10}200 = (\log_{10}a + kt)$	or $200 = "10^{\log a + kt}"$ oe
					200
				$\log 200 - 1.68$	$\log \frac{200}{47.0}$
		their 54	M1dep*	eg for their $t = \frac{10g 200^{\circ}}{0.0115}$	or M1 for their $t = \frac{47.9}{0.0115}$
			•	0.0115	0.0115
		2014 000	A1	if unsupported, allow B3 only if consistent with graph	
		2014 Cau		with graph	
			[3]		