\begin{tabular}{|c|c|c|c|c|c|c|}
\hline 1 \& ii
iii

iv \& \[
$$
\begin{aligned}
& \log _{10} P=\log _{10} a+\log _{10} 10^{b t} \\
& \log _{10} 10^{b t}=b t \\
& \text { intercept indicated as } \log _{10} a \\
& 3.9(0), 3.94,4(.00), 4.05,4.11 \\
& \text { plots ft } \\
& \text { line of best fit ft } \\
& \\
& \text { (gradient }=\text { ) } 0.04 \text { to } 0.06 \text { seen } \\
& \text { (intercept }=) 3.83 \text { to } 3.86 \text { seen } \\
& (a=) 6760 \text { to } 7245 \text { seen } \\
& P=7000 \times 10^{0.05 t} \text { oe } \\
& 17000 \text { to } 18500
\end{aligned}
$$

\] \& | M1 |
| :--- |
| M1 |
| A1 |
| A1 |
| B2 | \& | condone omission of base |
| :--- |
| to 3 sf or more; condone one error 1 mm ruled and reasonable $\begin{aligned} & 7000 \times 1.12^{t} \\ & \text { SC P = } 10^{0.05 t+3.85} \text { left A2 } \\ & 14000 \text { to } 22000 \mathrm{~B} 1 \end{aligned}$ | \& 3

3

4
2 \& 12 \\
\hline
\end{tabular}

| $\mathbf{2}$ | (i) <br> (ii) -2 <br> (iii) $\log x$ | 1 |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{3}$ | Correct curve thro' y axis <br> $(0,1)$ indicated on sketch or table <br> 5.64 | G1 <br> G1 | y, $y^{\prime} \& y^{\prime \prime}$ all positive <br> independent <br> M1 for $1 / 9=3^{-2}$ or $\log (1)-\log \left(3^{2}\right)$ <br> base not requd; M1 for $5 \log x$ or $\log \left(x^{6}\right)$ | 5 |


| 4 | i | 81 | 1 |  | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | ii | (1x) $3^{n-1}$ | 1 |  | 1 |
|  | iii | (GP with) $a=1$ and $r=3$ <br> clear correct use GP sum formula | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \end{aligned}$ | or M1 for $=1+3+9+\ldots+3^{n-1}$ | 2 |
|  | iv | (A) 6 www <br> (B) B) | $\begin{aligned} & 2 \\ & 1 \end{aligned}$ | M1 for $364=\left(3^{n}-1\right) / 2$ | 3 |
|  | v | $\begin{aligned} & \text { their (ii) }>900 \\ & (y-1) \log 3>\log 900 y \\ & -1>\log 900 \div \log 3 y \\ & =8 \text { cao } \end{aligned}$ | M1ft <br> M1ft <br> M1 <br> B1 | -1 once for $=$ or $<$ seen: condone wrong letter / missing brackets / no base | 4 |


| 5 | (i) |  | M1 | for curve of correct shape in both <br> quadrants <br> through (0, 1) shown on graph or in <br> commentary | SC1 for curve correct in 1 1t quadrant <br> and touching (0,1) or identified in <br> commentary |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 5 | (ii) | $5 x-1=\frac{\log _{10} 500000}{\log _{10} 3}$ <br> $x=\left(\frac{\log _{10} 500000}{\log _{10} 3}+1\right) \div 5$ <br> $[x=] 2.588$ to 2.59 | M1 | or $5 x-1=\log _{3} 500000$ | condone omission of base 10 <br> use of logs in other bases may earn <br> full marks |
| :--- | :--- | :--- | :---: | :--- | :--- |
| M1 | $x=\left(\log _{3} 500000+1\right) \div 5$ | A1 | oe; or B3 www |  |  |
| [3] |  | if unsupported, B3 for correct answer <br> to 3 sf or more www |  |  |  |


|  | (i | $\begin{aligned} & \log _{10} p=\log _{10} a+\log _{10} 10^{k t} \\ & \log _{10} p=\log _{10} a+k t \mathrm{www} \end{aligned}$ | M1 <br> A1 <br> [2] | condone omission of base; | if unsupported, B2 for correct equation |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | ( ii | $2.02,2.13,2.23$ <br> plots correct ruled line of best fit | $\begin{gathered} \text { B1 } \\ \text { B1f.t. } \\ \text { B1 } \\ \\ {[3]} \\ \hline \end{gathered}$ | allow given to more sig figs <br> to nearest half square $y$-intercept between 1.65 and 1.7 and at least one point on or above the line and at least one point on or below the line | $\begin{aligned} & \hline \text { 2.022304623..., 2.129657673, } \\ & 2.229707433 \\ & \text { ft their plots } \\ & \text { must cover range from } x=9 \text { to } 49 \end{aligned}$ |
| 6 | (iii | 0.0105 to 0.0125 for $k$ <br> 1.66 to 1.69 for $\log _{10} a$ or 45.7 to 49.0 for $a$ | $\begin{aligned} & \hline \hline \text { B1 } \\ & \text { B1 } \end{aligned}$ |  | must be connected to $k$ must be connected to $a$ |
|  |  | $\log _{10} p=\text { their } k t+\text { their } \log _{10} a$ $p=\text { their " } 47.9 \times 10^{00115 t ، \text { or } 10^{16785+0} 0115 t} \text { " }$ | B1 <br> B1 <br> [4] | must be a correct form for equation of line and with their $y$-intercept and their gradient (may be found from graph or from table, must be correct method) as above, " 47.9 " and " 0.0115 " must follow from correct method |  |
| 6 | (iv) | 45.7 to 49.0 million | 1 <br> [1] | 'million' needed, not just the value of $p$ |  |
| 6 | (v | reading from graph at 2.301.. <br> their 54 |  | or $\log _{10} 200={ }^{\prime} \log _{10} a+k t "$ <br> eg for their $t=\frac{\log 200-1.68}{0.0115}$ <br> if unsupported, allow B3 only if consistent with graph | or $200=" 10^{\log a+k t,}$ oe or M1 for their $t=\frac{\log \frac{200}{47.9}}{0.0115}$ |

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